Investigation of a probe design for facilitating the uses of the standard photon diffusion equation at short source-detector separations: Monte Carlo simulations

Sheng-Hao Tseng
National Cheng-Kung University
Department of Electro-Optical Engineering
1 University Road
Tainan, Taiwan 701

Carole Hayakawa
Jerome Spanier
Anthony J. Durkin
University of California, Irvine
Beckman Laser Institute
Laser Microbeam and Medical Program
1002 Health Sciences Road
Irvine, California 92617

Abstract. We design a special diffusing probe to investigate the optical properties of human skin in vivo. The special geometry of the probe enables a modified two-layer (MTL) diffusion model to precisely describe the photon transport even when the source-detector separation is shorter than 3 mean free paths. We provide a frequency domain comparison between the Monte Carlo model and the diffusion model in both the MTL geometry and conventional semi-infinite geometry. We show that using the Monte Carlo model as a benchmark method, the MTL diffusion theory performs better than the diffusion theory in the semi-infinite geometry. In addition, we carry out Monte Carlo simulations with the goal of investigating the dependence of the interrogation depth of this probe on several parameters including source-detector separation, sample optical properties, and properties of the diffusing high-scattering layer. From the simulations, we find that the optical properties of samples modulate the interrogation volume greatly, and the source-detector separation and the thickness of the diffusing layer are the two dominant probe parameters that impact the interrogation volume. Our simulation results provide design guidelines for a MTL geometry probe.

Keywords: tissue optics; near infrared spectroscopy; photon migration; Monte Carlo simulation.

Paper 09177R received May 7, 2009; revised manuscript received Aug. 26, 2009; accepted for publication Aug. 28, 2009; published online Oct. 30, 2009.

1 Introduction

Near-IR diffuse optical spectroscopy (DOS) is commonly used to determine in vivo tissue absorption coefficient $\mu_a$ and reduced scattering coefficient $\mu'_s$, from which tissue functional information, such as hemoglobin concentration, oxygen saturation, water concentration, and averaged scatter size and density can be deduced. Both of these parameters are important in noninvasive tissue diagnostics, since the scattering coefficient of tissue can provide information about the mean size of the tissue scatterers, while the absorption coefficient of tissue can be used to determine chromophore species and concentrations. The interrogation depth of DOS measurements is generally proportional to the source-detector separation of the probe employed and it also depends on the optical properties of tissues under investigation. DOS methods with source-detector separation larger than 20 mm have performed quite well in the 600 to 1000-nm spectral range for the purpose of determining optical properties and chromophore concentrations of thick tissues (depths greater than 10 mm) such as breast and brain. DOS techniques have been applied to investigate optical properties of superficial tissues as well. Bevilacqua et al. used a fiber probe having source-detector separations in the range from 0.3 to 1.4 mm along with a Monte Carlo model to recover optical properties of a human skull and brain. Bays et al. employed spatially resolved reflectometry to determine optical properties of human esophageal wall with a probe having source-detector separations ranging from 3 to 20 mm. Amelink et al. developed differential path-length spectroscopy to investigate optical properties of bronchial mucosa. In all cases, DOS techniques require either a photon transport model or an empirical model to determine $\mu_a$ and $\mu'_s$ from the reflectance.

The photon transport model most often utilized for determining optical properties from DOS measurements is the standard diffusion model derived from the radiative transport theory. Because of its simplicity and computational efficiency, the standard diffusion model has been used widely and successfully to recover optical properties of deep tissues. While the standard diffusion model is derived from the radiative transport theory with diffusion approximations, the model cannot be used reliably for recovering the optical properties of...
typical biological tissues when \((p/l)\) is smaller than 10, where \(p\) is the source-detector separation and \(l\) is the transport mean free path \(1/(\mu_s + \mu'_s)\). To reliably determine optical properties of superficial tissue volumes lying between the tissue surface and 1 to 2 mm deep using DOS, measurements with source-detector separation shorter than 3 mm are necessary. This regime is of great interest for skin-cancer-oriented applications, oral cancer applications, and numerous applications accessible via endoscope in which functional characterization of tissue is desirable. Several alternative approaches to diffusion approximation such as Monte Carlo simulations, \(P_3\) approximation, and \(\delta-P_3\) approximation have been proposed for short source-detector separation DOS applications.

Although methods based on Monte Carlo techniques have, in certain circumstances, been shown to provide the most accurate results among the aforementioned models, the need for intensive computation resources to build a data library in advance limits its applicability. Several researchers have developed the so-called “white Monte Carlo model,” which enables the calculation of optical properties based on a single Monte Carlo simulation to bring the computation time similar to the diffusion theory based models. However, it is shown that even with the white Monte Carlo method, a data library containing various single scattering phase functions still must be established in advance to recover optical properties of superficial tissues, since the single scattering phase function of tissue actively affects the measured reflectance especially when the source-detector separation is shorter than 1 to 2 mm. By changing the scattering phase function used in the Monte Carlo model, Liu and Ramanujam reported the reflectance generated with different scattering phase functions could have deviation larger than 20% at source-detector separations shorter than 1 mm. This deviation in calculated reflectance resulted in 31.4% error in the recovered absorption coefficient. In contrast, the diffusion-based models do not require a phase function to recover \(\mu_s\) and \(\mu'_s\). We demonstrated that using a novel optical probe to facilitate the usage of the diffusion model to recover the optical properties of superficial volume of a tissue phantom \((\mu'_s/\mu_s = 25)\) with less than 8% error.

The diffusing probe we proposed employs a slab of highly scattering Spectralon (Labsphere, New Hampshire) \((\mu'_s \sim 50/\text{mm}, \mu_s \sim 10^{-6}/\text{mm})\) that is placed in contact with the surface of the sample under investigation (Fig. 1). This scattering layer causes photons emitted from the source optical fiber to undergo multiple scattering. This enables us to employ a modified two-layer (MTL) standard diffusion model to recover the sample optical properties, even under the condition that the source-detector separation is less than 3 transport mean free paths.

We successfully applied the diffusing probe to study the optical properties of in vivo human skin. We are planning to use the diffusing probe in many clinical applications. To correctly interpret in vivo measurement results obtained from the diffusing probe, it is critical to characterize and understand the effects of parameters of the diffusing probe that may impact the interrogation volume. The primary objective of this paper is to methodically examine the influence of sample optical properties and probe parameters on the depth of interrogation of the diffusing probe.

In this paper, we first demonstrate the accuracy and the advantage of the MTL diffusion model over a standard diffusion approach. The performance of the diffusion model, in either MTL geometry or seminfinite geometry, was evaluated by a benchmark Monte Carlo model. While the reflectance generated from the Monte Carlo model is sensitive to the choice of the scattering phase function when the source-detector separation is smaller than 1 mm, the Monte Carlo model is usually employed as the gold standard method to calculate diffuse reflectance when the source-detector separation is larger than 1 mm. It was reported that when using different scattering phase functions in the Monte Carlo model, the difference in generated reflectance was less than 10% when the source-detector separation was larger than 1 mm. Thus, in this study, to use the Monte Carlo model as a benchmark method, we limit the source-detector separations to be larger than 1 mm in all simulations.

We also conducted numerous Monte Carlo simulations with the objective of investigating the dependence of the probing depth of the diffusing probe on the optical properties of samples, scattering, absorption, and thickness of the diffusing layer of the probe, as well as dependence on the source-detector separation. The simulation results presented provide design guidelines for a diffusing probe having specific interrogation depth characteristics.

### 2 Materials and Methods

The superficial diffusing probe employs a source fiber that is coupled to a high-scattering, low-absorption Spectralon slab having known optical properties. Light must pass from the fiber, through the diffusing slab, and into the tissue that is being measured. The detection fiber penetrates the slab and is in contact with the sample, as shown in Fig. 1. In this geometry, the measured reflectance is described using a MTL diffusion model derived from a standard two-layer diffusion model. Previously, we demonstrated that the diffusing probe can be used to accurately determine optical properties of homogeneous tissue phantoms at 660 nm and human skin in the range from 650 to 1000 nm.
To quantitatively evaluate the accuracy of the MTL diffusion model and estimate the effects of various parameters on the interrogation depth of the diffusing probe, we carried out a series of Monte Carlo simulations. The Monte Carlo code used here is an extension of the general multilayer, 3-D, weighted photon Monte Carlo code developed by Wang et al. Kienle and Patterson indicated that the asymmetry parameter of tissue is normally greater than 0.8, and an asymmetry parameter between 0.8 and 1 does not significantly influence the reflectance when $\mu'_a$ is constant. Therefore, for all simulations, we employed a Heney-Greenstein phase function and used an asymmetry parameter of 0.8 for all layers to speed up computation. In the simulations, the optical properties of the diffusing layer (Spectraplan) was set at $\mu_a = 10^{-6}/\text{mm}$, and $\mu'_a = 50/\text{mm}$. The lateral dimensions of the diffusing layer and samples were set to $10^3 \times 10^3 \text{cm}^2$ to simulate infinite lateral dimensions of the diffusing layer and samples. Samples were assumed to be homogenous with a thickness of 10 cm. In reality, the radius of the diffusing slab in the 3-mm-source-detector-separation diffusing probe is about 5 mm, and this diffusing probe has been demonstrated to be able to precisely recover sample optical properties with a MTL diffusion model.

In this paper, we will first evaluate the performance of the MTL diffusion model and compare it to the diffusion model in seminfinite geometry. We utilize the Monte Carlo model, which is in either MTL geometry or seminfinite geometry, to generate a benchmark frequency domain reflectance that contains phase and amplitude information. Therefore, we can quantitatively calculate the deviation of the frequency domain reflectance generated from the diffusion model, in either geometry, from the benchmark values.

Second, we vary sample optical properties, source-detector separation, and the properties of the diffusing slab in the Monte Carlo model to understand their effect on the interrogation depth of the diffusing probe. We describe the interrogation depth of each Monte Carlo simulation in the following manner. Let $P_i = W_i / \sum_{j=1}^{m} W_j$, where $W_i$ is the final weight of a detected photon packet, and $n$ is the number of photon packets launched. The average interrogation depth of a simulation is determined as $z_{ave} = \sum_{j=1}^{m} d_j / m$, where $d_j$ is the depth at which a collision happens in the sample, and $m$ is the total collision number in the sample of the detected photon packet. The standard deviation of each simulation is also calculated, which represents the variance of the result.

Moreover, to visualize the distribution of detected photon packets in the superficial diffusing probe geometry, we generate 2-D fluence distribution maps using Monte Carlo simulations. When a photon packet undergoes a collision, a fraction of energy of the photon packet, which is proportional to the weight of the photon packet and the absorption of the medium, is deposited to a local voxel in a 3-D Cartesian coordinate system. Voxel size is set to be 0.05 mm$^3$ or 0.1 mm$^3$ when the source-detector separation is 1 or 5 mm, respectively, in our simulations. Local fluence (in joules per square millimeter) is calculated by dividing the deposited energy by the local absorption coefficient. A 3-D photon fluence distribution map is obtained by accumulating the fluence distribution of all photon packets arriving at the detector. The 3-D map is converted to a 2-D x-z map by binning along the y axis. The maps are normalized by the number of photon packets launched and the volume of a voxel. The photon fluence maps presented here are plotted as logarithm base 10 for greater ease of visualization.

To achieve a relative standard deviation in the predicted reflectance of <5%, a total of 50 million photons were launched in each Monte Carlo simulation for calculating the average interrogation depth unless noted otherwise. Depending on the input parameters, between 10 to 20 h were required to complete a single simulation on an AMD Athlon FX-60-based PC. On the other hand, 50 million photon packets were used in each Monte Carlo simulation for calculating the fluence distribution map, and each required about 60 to 80 h to complete on an AMD Athlon FX-60-based computer. The value of each pixel in the map represents the average fluence of a certain volume.

### 3 Results and Discussion

#### 3.1 Comparison between the Monte Carlo Model and the Diffusion Model

In this section, we demonstrate the accuracy of reflectance generated from the MTL diffusion model. Results obtained from the Monte Carlo model were used here as a benchmark. In addition, the advantages of using the MTL diffusion model over the conventional diffusion model is discussed.

The Monte Carlo method and the diffusion model were employed to calculate the frequency domain diffuse reflectance in both the MTL geometry and the conventional semiinfinite geometry. In the simulations, the source-detector separation and the thickness of the diffusing layer were 1 and 1.5 mm, respectively. Tissue samples had optical properties of either light skin or dark skin. The optical properties of light skin and dark skin used here were extracted from the ex vivo study conducted by Simpson et al. The optical properties of light skin and dark skin were $\mu_a = 0.05/\text{mm}$ and $\mu'_a = 0.3/\text{mm}$ and $\mu_a = 0.3/\text{mm}$ and $\mu'_a = 3/\text{mm}$, respectively, at a wavelength of 650 nm. Note that these properties agree with those that we have measured in vivo using a probe based on the MTL geometry. Amplitude demodulation and phase delay were determined in the source modulation frequency range within 50 to 1000 MHz since our frequency domain photon migration (FDM) instrument is capable of operating over this range of frequencies. The amplitude demodulation and phase delay reported by Monte Carlo simulations and the diffusion model in the MTL geometry and seminfinite geometry are shown in Figs. and respectively. In Figs. and the maximum percentage deviations of amplitude demodulation and phase delay of the MTL diffusion model from the Monte Carlo simulation results are less than 0.3 and 1.3%, respectively. In contrast, the conventional semiinfinite diffusion model generated amplitude demodulation and phase delay deviation from the Monte Carlo simulation results within 0.1 and 6.3%, respectively.

The results obtained using the diffusion model in the MTL geometry deviate by a smaller amount from the Monte Carlo model than do the results obtained for the diffusion model in the semi-infinite geometry. In the MTL geometry, the Spectralon layer diffuses the photons emitted from the source fiber,
the photons leaving Spectralon and entering tissue sample have a widely varying initial incident angle to the tissue sample surface (this phenomenon can be visually seen in the photon fluence distribution maps that will be shown and discussed shortly). In contrast, in the semiinfinite geometry, all photons from the source fiber have the same incident angle to the detector in these two geometries are much different. From Monte Carlo simulations, we determined that the mean of total path lengths in the sample volume are 6.1 and 4.3 mm for the MTL geometry and the semiinfinite geometry, respectively, when the source-detector separation was 1 mm and the sample had optical properties of light skin. A longer traveling distance in the sample layer when the MTL geometry is employed means that light propagation in this geometry more closely mimics diffusion. The difference in traveling distance is 1.8 mm, which is equivalent to 5.5 transport mean free paths in a medium that has optical properties of $\mu_s = 0.05$ mm and $\mu'_s = 3$ mm. This explains the reason for the diffusion model performing better in the MTL geometry than in the semiinfinite geometry at a certain source-detector separation.

In addition, from our simulation results (which are shown in Fig. 10 and 11 in Sec. 3.5), we found that the interrogation depth of the MTL geometry is 25 to 30% smaller than that of...
the conventional semiinfinite geometry, at source-detector separations of either 1 or 5 mm. From the Monte Carlo simulations, it was found that most of photons have oblique incidence angles from the diffusing layer to the tissue layer in the MTL geometry. Therefore, photons have shallower interrogation depths in the MTL geometry than in the conventional semiinfinite geometry. This property makes the MTL geometry very suitable for investigating superficial volume of tissues.

Although the MTL diffusion model results are more accurate than those for the conventional semiinfinite diffusion model results, the conventional semiinfinite diffusion model results deviate from the Monte Carlo results by less than 7%, which is not a large number for computing reflectance. Many researchers have also reported that the standard diffusion model deviates from Monte Carlo simulations by less than 5% even when the ratio of source-detector separation to transport mean free path \((p/l)\) is close to 1. This means that, theoretically, a diffusion model in semiinfinite geometry can work properly in recovering sample optical properties even at the source-detector separation of 1 mm. This also means that the MTL diffusion model may have similar performance compared to the diffusion model in semiinfinite geometry in recovering sample optical properties from experiment data. However, experimentally, we have found that the diffusion theory in the MTL geometry could accurately recover optical properties of tissue phantoms within 8% deviation with a 2.5-mm source-detector separation, while the optical properties of the same phantoms recovered by diffusion theory in the semi-infinite geometry had maximum deviations of 60 to 100% when the source-detector separation was 5 mm (Ref. 16). Yoo et al. reported that, in the time-domain with \((p/l)\) smaller than 10, none of the theoretical data from the diffusion theory agrees with experimental results. Martelli et al. showed that the \(\mu'\) recovered from time-domain experiment data using the diffusion theory had about 8% error even when the \((p/l)\) is 10 and \(\mu_s\) is 0. Both the model error resulting from the semiinfinite geometry diffusion theory and the measurement error resulting from the instruments contribute to the large deviation of experimentally recovered values from the true values. Thus, it can be concluded that the accuracy of applying the diffusion model to recover the experimental data is not commensurate with that predicted by computer simulations. Since the diffusion model in MTL geometry theoretically and experimentally performs better than the diffusion model in semiinfinite geometry at short source-detector separations, the diffusing probe is very suitable for studying in vivo superficial tissues. In the next few sections, we demonstrate the effect of several parameters on the interrogation depth of the diffusing probe. Our simulation results can provide a design guideline for a MTL geometry probe for a specific application.

### 3.2 Effects of Source-Detector Separation

Because the MTL probe concept originates from a desire to rapidly measure local optical properties close to the source, we limit the analysis of source-detector separation to the 1 to 5-mm range. A detailed analysis of this range follows. We have estimated the attenuation of light from source to detector in this geometry using Monte Carlo simulations of the MTL probe. The attenuation results as a function of source-detector separation are listed in Table 1. In the simulations, the source-detector separation was either 1 or 5 mm, the Spectralon thickness was 1.5 or 3 mm, and tissue samples had optical properties of light skin \((\mu_a=0.05/mm\) and \(\mu'_s=3/mm\)) or dark skin \((\mu_a=0.3/mm\) and \(\mu'_s=3/mm\)).

<table>
<thead>
<tr>
<th>Source-Detector Separation</th>
<th>Attenuation (dB)</th>
<th>Light Skin</th>
<th>Dark skin</th>
</tr>
</thead>
<tbody>
<tr>
<td>SD=1 mm, t=1.5 mm</td>
<td>22</td>
<td>24</td>
<td></td>
</tr>
<tr>
<td>SD=5 mm, t=1.5 mm</td>
<td>40</td>
<td>55</td>
<td></td>
</tr>
<tr>
<td>SD=1 mm, t=3.0 mm</td>
<td>28</td>
<td>31</td>
<td></td>
</tr>
<tr>
<td>SD=5 mm, t=3.0 mm</td>
<td>40</td>
<td>47</td>
<td></td>
</tr>
</tbody>
</table>

In the simulations, the source-detector (SD) separation was 1 or 5 mm, the Spectralon thickness was 1.5 or 3 mm, and tissue samples were assigned optical properties corresponding to light skin or dark skin as defined in the Sec. 2. In our previous in vivo study, we employed a diffusing probe with 1.5-mm thick Spectralon to successfully recover the optical properties of skin. Here, we have defined the Spectralon thicknesses to be 1.5 as well as 3 mm to understand the influence of the thickness of the Spectralon on the signal attenuation.

Simulation results shown in Table 1 indicate that when the Spectralon layer is 1.5 mm thick, the attenuations are 22 and 40 dB for light skin at 1 and 5-mm source detector separations, respectively. In a typical frequency domain DOS system such as the one used in our lab, laser diodes deliver about 10 mW of power into the sample. For such a system, with attenuation consistent with that estimated from Monte Carlo simulations, this means that the light intensities will be about −12 and −30 dBm at the detector for source-detector separations of 1 and 5 mm, respectively. If, on the other hand, the sample is similar to dark skin (as described in Sec. 2), the estimated attenuations will be in the range of 24 and 55 dB at 1- and 5-mm source-detector separations respectively. Using our frequency domain DOS system as an example, this will result in a light intensities of −14 and −45 dBm at the detector, respectively.

A typical detector used in the frequency domain DOS measurement is the Hamamatsu APD (model# C5658, Hamamatsu, New Jersey), which has noise level of around −48 dBm. Therefore, a 5-mm source-detector separation is about the largest distance one can use in the frequency domain measurements with this probe design. This is in agreement with our experience in terms of using this probe to measure in vivo skin. Interestingly, at a source-detector separation of 5 mm, the estimated attenuation is reduced when the Spectralon layer thickness is adjusted from 1.5 to 3 mm for measuring dark skin. Because Spectralon essentially doesn’t absorb light \((\mu'_l \sim 50/mm\) and \(\mu_a \sim 10^{-6}/mm\)), when it is thicker, more photons will travel in the Spectralon longer in terms of time, to take a “shortcut” of sorts, leaving the Spectralon at a location near the detector, passing through very little sample, and finally arriving at the detector. When photons travel in a sample having a high ab-

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Table 1: Light attenuation of the MTL geometry calculated with Monte Carlo simulations.
sorption coefficient, such as dark skin, such a “shortcut” can result in photons experiencing less absorption before they arrive at the detector than they would have experienced for a thinner slab of Spectralon. Hence, the estimated attenuation at a source-detector separation of 5 mm is greater for 1.5-mm-thick Spectralon than it is for 3-mm-thick Spectralon (all other things being equal) when the sample under investigation has high absorption. On the other hand, the loss of photons introduced by the high scattering of the Spectralon is still significant to the system. Therefore, when the sample has moderate absorption, which is the case with light skin, the “shortcut” effect is not obvious, as demonstrated in Table 3.5. From Table 3.5 for skin applications and assuming the scattering coefficient for all skin prototypes is the same, the absorption coefficient of 0.05/μm is the threshold point to observe this phenomenon. We show more simulation results to elaborate on this in a later section (and in Fig. 6 in Sec. 3.3 and Fig. 5 in Sec. 3.4).

3.3 Interrogation Depth: Role of Sample Optical Properties and Source-Detector Separation

It is known that the optical properties of tissue influence the interrogation depth of DOS techniques. Because the geometry that we have introduced is somewhat unusual, it is not necessarily obvious how the interrogation depth will be affected by sample optical properties. Hence, Monte Carlo simulations were carried out in an effort to determine the average interrogation depths of the superficial diffusing probe for near-IR optical properties corresponding to those of various biological tissues. The range of sample optical properties used in the simulations was carefully chosen based on a survey of the literature so as to be inclusive of superficial tissues optical properties in the 600 to 1000-nm wavelength range. Hornung et al. reported that the optical properties of cervical tissues are in the range from 0.015/mm to 0.019/mm for μa and 0.84/mm to 0.90/mm for μs at the wavelength of 674 nm. Bays et al. determined the optical properties of human esophageal wall to be μa~0.26/mm and μs~0.71/mm at the wavelength of 633 nm. Simpson et al. performed measurements on skin and showed that the optical properties are μa=0.3/mm and μs~3/mm and μa~0.05/mm and μs~3/mm for African and Caucasian skin, respectively, at a wavelength of 650 nm. Based on these results, the range of optical properties used here was 0.01/mm<μa<0.5/mm and 0.5/mm<μs<5/mm. Indices of refraction of the scattering slab and the sample were taken to be 1.35 and 1.37, respectively.

Figures 5(a) and 5(b) (in the next paragraph) illustrate variation in estimated average interrogation depth as a function of sample optical properties for the source-detector separations of 1 and 5 mm, respectively. The circles shown in Fig. 4 are the data generated from Monte Carlo simulations. In general, the interrogation depth increases as absorption and reduced scattering coefficients decrease. When the source-detector separation is 5 mm, the average interrogation depth varies from 1766 to 141 μm as the optical properties vary from μa=0.01/mm and μs=0.5/mm (low absorption, low scattering) to μa=0.5/mm and μs=5/mm (high absorption, high scattering). When the source-detector separation is 1 mm, the average interrogation depth varies from 657 to 96 μm as the optical properties vary from μa=0.01/mm and μs=0.5/mm (low absorption, low scattering) to μa=0.5/mm and μs=5/mm (high absorption, high scattering). We also employed the nonlinear surface fitting tool from OriginPro 8 (OriginLab Co., Massachusetts) to find two functions that best describe the data points shown in Figs. 4(a) and 4(b). We found the following equation that well relates the interrogation depth (Z) to the optical properties (μa and μs) of samples:

\[
Z = z_0 + A01(μ_a) + B01(μ'_s) + B02(μ'_a)^2 + B03(μ'_s)^3
= 1 + A1(μ_a) + A2(μ_a)^2 + A3(μ'_s)^3 + B1(μ'_s) + B2(μ'_a)^2
\]

(1)

For the data shown in Fig. 4(a) we obtained the following fitting parameter values: \(z_0 = 889.2564\), \(A01 = 13.05555\), \(A1 = 0.345\), etc.
B01 = −306.09145, B02 = 75.63521, B03 = −7.20714, A1 = 14.14781, A2 = −36.73759, A3 = 39.38632, B1 = 0.04375, and B2 = −0.01240. For the data shown in Fig. 4, we obtained the following fitting parameter values: $z_0 = 2265.00667$, A1 = −996.31590, B01 = −887.58451, B02 = 218.58048, B03 = −20.33626, A1 = 11.22803, A2 = −35.76202, A3 = 37.73542, B1 = −0.07432, B2 = −3.75 $\times 10^{-6}$. The surfaces demonstrated in Figs. 4(a) and 4(b) are the fitting results based on Eq. (1) and the parameter values listed in the preceding.

Figure 5 shows Monte Carlo simulation results that illustrate average interrogation depth versus source-detector separation for samples having optical properties of light and dark skin as described earlier. The average interrogation depth increases linearly with source-detector separation in the range from 1 to 5 mm, despite differences in optical properties of samples. Monte Carlo simulations were used by other groups to aid in probe design. In practice, Eq. (1) and Fig. 5 can be used to guide the design of the diffusing probe for a particular application. For example, to achieve similar interrogation depth when applying the diffusing probe to study light skin and dark skin, according to Fig. 5, one could use diffusing probes of 1 and 3 mm source-detector separations to study light skin and dark skin, respectively, to obtain an interrogation depth of around 250 μm.

From Fig. 5, it can be clearly seen that the source-detector separation is a dominant factor that can modulate the interrogation depth of the diffusing probe. To visualize the effect of adjusting the source-detector separation on the sampling region, Fig. 6 illustrates Monte Carlo simulated photon fluence distribution maps for a sample having optical properties mimicking light skin ($\mu'_a = 0.05/\text{mm}$ and $\mu'_s = 3/\text{mm}$) measured in the MTL geometry, which has a Spectralon thickness of 1.5 mm and a source-detector separation of 1 or 5 mm. Other parameters used in the simulations were consistent with those used to generate Fig. 5. In general, Fig. 6 shows that the interrogation region of a diffusing probe has the shape close to a semi-oval. The photon fluence distribution in the sample for a 5-mm source-detector separation diffusing probe is wider and deeper than that for a 1-mm source-detector separation diffusing probe. In Figs. 6(a) and 6(b), the magnitude of the photon fluence beneath the detector of the 5-mm source-detector separation probe is weaker than that of the 1-mm source-detector separation probe by a factor of 100. The rapid decline in detected photon fluence as the source-detector separation increases limits the largest source-detector separation that can be employed in real measurements.

### 3.4 Interrogation Depth versus Absorption, Scattering, and Thickness of the Scattering Layer

In this section, we investigate the influence of probe parameters related to the diffusing layer on the interrogation depth of the diffusing probe. Figure 7 shows the simulated dependence of the interrogation depth of the diffusing probe on the diffusing slab thickness and the absorption coefficient at source-detector separations of 1 and 5 mm. The sample optical properties employed here are those of light and dark skin as detailed in the previous subsection.

For the purposes of these simulations, the $\mu'_a$ of the diffusing layer was varied from $10^{-5}$/mm to $10^{-3}$/mm. In Figs. 8(a) and 8(b), the simulation results illustrate that a variation of less than 0.1% in interrogation depths was introduced by varying the absorption coefficient of the scattering slab for different probe source-detector separations and sample optical properties. Absorption coefficients larger than $10^{-3}$/mm were not considered here since the purpose of employing a scattering slab is to cause photons to undergo many scattering collisions at very short distances from the source. Increasing the absorption coefficient of the slab would increase competition between absorption and scattering and attenuate the detected signal. The absorption of the scattering slab in the range considered has almost no influence on the average interrogation depth of the diffusing probe. This suggests that the absorption of the scattering slab within this limited range of absorption values has a negligible effect on the fluence distribution of the detected photons in the scattering slab. Using a slab with an absorption coefficient as small as possible is beneficial for maximizing the detected reflectance signal.

The results presented in Fig. 7 suggest that the interrogation depth of the diffusing probe can be affected by the thickness of the scattering slab. Figure 7(a) shows that when employing a 1-mm source-detector separation diffusing probe to measure light skin and the thickness of the scattering slab is adjusted from 1.5 to 3 mm, the average interrogation depth increases by 25 μm. On the other hand, in Fig. 7(b), the average interrogation depth decreases by 220 μm when a 5-mm source-detector separation diffusing probe is applied to measure light skin and the thickness of scattering slab is adjusted from 1.5 to 3 mm. The range of variation of interrogation depth introduced by adjusting the scattering slab thickness is larger for the 5-mm source-detector separation diffusing probe than that for the 1-mm source-detector separation diffusing probe. In addition, the trends in the variation of the interrogation depths are opposite for these two cases. This is reinforced with two additional photon fluence distribution maps as shown in Fig. 8. Figures 8(a) and 8(b) depict simulated photon fluence distribution maps for probes having a

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**Fig. 5** Average interrogation depth versus the source-detector separation. Triangles and circles represent the interrogation depth of the diffusing probe applied to dark skin ($\mu'_a = 0.3/\text{mm}$ and $\mu'_s = 3/\text{mm}$) and light skin ($\mu'_a = 0.05/\text{mm}$ and $\mu'_s = 3/\text{mm}$), respectively. The two straight lines are fit to the data. The thickness of the diffusing slab is 1.5 mm, and the optical properties of the slab are $\mu'_a = 10^{-6}/\text{mm}$ and $\mu'_s = 50/\text{mm}$. The asymmetry factor $g$ is 0.8 for both layers. The error bars represent standard deviation.

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**Fig. 6** Illustrates Monte Carlo simulated photon fluence distribution maps for a sample having optical properties mimicking light skin ($\mu'_a = 0.05/\text{mm}$ and $\mu'_s = 3/\text{mm}$) measured in the MTL geometry, which has a Spectralon thickness of 1.5 mm and a source-detector separation of 1 or 5 mm. Other parameters used in the simulations were consistent with those used to generate Fig. 5. In general, Fig. 6 shows that the interrogation region of a diffusing probe has the shape close to a semi-oval. The photon fluence distribution in the sample for a 5-mm source-detector separation diffusing probe is wider and deeper than that for a 1-mm source-detector separation diffusing probe. In Figs. 6(a) and 6(b), the magnitude of the photon fluence beneath the detector of the 5-mm source-detector separation probe is weaker than that of the 1-mm source-detector separation probe by a factor of 100. The rapid decline in detected photon fluence as the source-detector separation increases limits the largest source-detector separation that can be employed in real measurements.
A 3-mm-thick scattering slab and with source-detector separations of 1 and 5 mm, respectively. Other parameters are identical to those used to generate Fig. 6. Comparing Fig. 6 and Fig. 8, it is clear that the interrogation region is widened when the scattering slab thickness of a 1-mm source-detector separation diffusing probe increases from 1.5 to 3 mm. Increasing slab thickness results in greater lateral propagation of light. The positions of the detectors are fixed at 1 mm from the source in both Fig. 6 and Fig. 8. Thus, in Fig. 8, as photons propagate laterally more than 2 mm from the source in the scattering slab, photons have to travel in the sample at a depth that is more than the average depth determined in the Fig. 6 before they arrive at the detector. Therefore, the interrogation depth of a 1-mm source-detector separation diffusing probe increases as the thickness of the scattering slab increases from 1.5 to 3 mm.

In contrast, when the source-detector separation is 5 mm, the magnitude of the photon fluence in the scattering slab at the lateral position of the detector is greater in Fig. 8 than that in Fig. 6. As the thickness of the scattering slab increases, so does the number of photons that travel through the slab to positions near the detector before entering the sample. Those photons will be more likely to travel superficial trajectories in the sample prior to detection. Accordingly, the interrogation region becomes more concentrated near the top of the sample as the thickness of the scattering slab of a 5-mm source-detector separation diffusing probe is increased from 1.5 to 3 mm.

The detailed dependence of the interrogation depth on the scattering slab thickness for various source-detector separations is shown in Fig. 9. For this set of simulations, the thickness of the scattering slab is varied from 0.75 to 3 mm while the source-detector separation is varied from 1 to 5 mm. The reason for setting the lower bound and upper bound of the Spectralon thickness to 0.75 and 3 mm, respectively, is to understand the effect of varying the Spectralon thickness of the currently working prototype, which has a 1.5-mm Spectralon thickness. The optical properties of the scattering slab and the sample are \( \mu_a = 10^{-6} / \text{mm} \) and \( \mu'_a = 50 / \text{mm} \), and \( \mu_s = 0.05 / \text{mm} \) and \( \mu'_s = 3 / \text{mm} \), respectively. It can be seen that the thickness of the scattering slab has a relatively smaller influence on the interrogation depth of a 1-mm source-detector separation diffusing probe compared to 3- and 5-mm source-detector separation diffusing probes. For probes having source-detector separations of 3 and 5 mm, the interrogation depth increases as the scattering layer thickness decreases, as shown in Figs. 6(b) and 8(b).

We also carried out a series of Monte Carlo simulations to study the dependence of the interrogation depths of the diffusing probes on the scattering slab thickness.
To make the diffusion approximation valid in the case where photons transmitting through a slab consist of scatters and absorbers, the slab must have the reduced scattering coefficient much greater than the absorption coefficient and the slab thickness should be larger than $R_{m}$, where $R_{m} = 1/(\mu_s + \mu'_s)$ is the transport mean free path. Thus, when designing the probe, one must consider both the thickness and the $\mu'_s$ of the diffusing layer to meet the requirements for validity of the diffusion approximation. The thinnest diffusing layer that satisfies the diffusion approximation can therefore be estimated to be 0.16 mm when the $\mu'_s$ of the slab (Spectralon) is 50/\(\text{mm}\) at 650 nm. Practically, when choosing the scattering slab thickness for a probe, in addition to the validity of the diffusion approximation, the limitations in fabrication and material, such as rigidity of the Spectralon slab and the robustness of the probe, should also be taken into account. We have found that a Spectralon slab with a 1.5-mm thickness can be used to reliably fabricate a probe for skin measurements. In principle, any material with high scattering and low absorption properties can be used as the scattering slab in a diffusing probe. The thickness of the material should be determined based on the scattering property and the mechanical strength of the material, which affect the validity of the diffusion approximation and probe reliability, respectively.

### 3.5 Interrogation Depths versus Numerical Aperture and Phase Function of the Scattering Layer

We also investigated the influence of the numerical aperture (NA) of fibers on the interrogation depth. Simulations were carried out using 1- and 5-mm source-detector separations for a 1.5-mm scattering slab thickness. One hundred million photons were used in the simulations to achieve a standard deviation smaller than 3%. The optical properties of the scattering slab and the sample were $\mu_a=10^{-6}/\text{mm}$ and $\mu'_s=50/\text{mm}$ and $\mu_a=0.05/\text{mm}$ and $\mu'_s=3/\text{mm}$, respectively. The NA of detection and source fibers was varied from 0.2 to 1.35. Indices of refraction of the scattering slab and the sample were 1.35 and 1.37, respectively. The simulation results are shown in Fig. 10. The average interrogation depth decreases as the numerical aperture of detection fiber increases. This trend holds for SD=1 mm but not for SD=5 mm, where SD is source-detector separation. Note that when the NA of fiber decreases from 1.35 to 0.2 and source-detector separation is 1 mm, the average interrogation depth increases by ~5% with standard deviation of 2 to 3%. With the same setup, the average interrogation depth of a semiinfinite geometry probe with 1-mm source-detector separation versus the NA of detection fiber is shown in Fig. 11. The variation of the interrogation depth is about 10% when the NA of detection fiber is changed from 0.2 to 1.35. Compared to the semiinfinite geometry, the interrogation depth of the MTL geometry has a weak dependence on the NA of the detection fiber. Both the MTL geometry and the semiinfinite geometry lose the dependence of interrogation depth on the NA of detection fiber when the source detector separation is increased to 5 mm. Although the NA has been shown to have moderate influence on the interrogation depth of the semiinfinite probing geometry, the weak influence of NA on the interrogation depth of the MTL geometry makes it a less effective parameter in modulating the probing depth on the NA of detection fiber when the source detector separation is increased to 5 mm.
depth compared to the source detector separation and the scattering layer thickness layer thickness. Note again that, as shown in Figs. 10 and 11, the interrogation depth of the MTL geometry is, in general, 25 to 30% shallower than that of the semiinfinite geometry at the same source-detector separation. This result is caused by the oblique incidence angle of photons traveling from the diffusing layer to the tissue layer in the MTL geometry. Similar phenomenon has been reported by Wang et al.

Finally, since the reduced scattering coefficient can be expressed as $\mu'_s = \mu_s (1 - g)$, where $\mu_s$ is the scattering coefficient, and $g$ is the asymmetry factor, one might wonder about the effect of $g$ of the scattering slab on the interrogation depth of the probe. We carried out Monte Carlo simulations to calculate the average interrogation depths for the asymmetry factor of the scattering slab ranging from 0.01 to 0.9. The scattering slab thickness was 1.5 mm and the optical properties of the scattering slab and the sample were $\mu_s = 10^{-6}$/mm and $\mu'_s = 50$/mm and $\mu_s = 0.05$/mm and $\mu'_s = 3$/mm, respectively. The average interrogation depth was determined as $273 \pm 15$ and $763 \pm 16$ μm for source-detector separations of 1 and 5 mm, respectively. When the asymmetry factor is varied from 0.01 to 0.9, the interrogation depth is not affected by the asymmetry factor of the scattering slab despite using different source-detector separations. However, our simulation results indicate that the detection efficiency is decreased by a factor of 10 when the asymmetry factor is varied from 0.9 to 0.01. Thus, choosing a scattering material with high asymmetry factor number, such as Spectralon or white Delrin, as the diffusing layer of a diffusing probe is advantageous for promoting the photon detection efficiency.

In addition, we also carried out a series of Monte Carlo simulations to investigate the effect of the asymmetry factor of tissue samples on the interrogation depth of the diffusing probe.
probe. In the simulations, we designed the tissue asymmetry factors to be in the range from 0.8 to 0.99. Other parameters were the same as those already mentioned. When the source-detector separation was 1 mm, the interrogation depths were determined to be $274 \pm 3 \mu m$. Our simulation results infer that the influence of the tissue asymmetry factor on the interrogation depth of the diffusing probe is weak. Therefore the simulation results shown in this work can also apply to the cases where the asymmetry factor of superficial tissues is higher than 0.8.

![Fig. 9](image1.png) Average interrogation depth versus thickness of the diffusing slab. The source-detector separations employed in the simulations are 1 (square), 3 (circle), and 5 mm (triangle). The optical properties of the slab and the sample are $\mu_s = 10^{-6}/\text{mm}$ and $\mu_s' = 50/\text{mm}$ and $\mu_a = 0.05/\text{mm}$ and $\mu_a' = 3/\text{mm}$, respectively. The asymmetry factor $g$ is 0.8 for both layers. The error bars represent standard deviation.

![Fig. 10](image2.png) Average interrogation depth versus numerical aperture of fibers. The source-detector separations are 1 (lower plot) and 5 mm (upper plot). The optical properties of the slab are $\mu_s = 10^{-6}/\text{mm}$ and $\mu_s' = 50/\text{mm}$. The scattering slab thickness is 1.5 mm. The asymmetry factor $g$ is 0.8 for both layers. The error bars represent standard deviation.

![Fig. 11](image3.png) Average interrogation depth versus numerical aperture of fibers in the conventional semi-infinite geometry. The source-detector separations are 1 (lower plot) and 5 mm (upper plot). The asymmetry factor $g$ is 0.8. The error bars represent standard deviation.

### 4 Conclusion

We used the results of Monte Carlo simulations to characterize and illustrate the properties of the MTL geometry and contrast this to conventional semi-infinite geometry. We found that the diffusion theory performs better in the MTL geometry than in the conventional semi-infinite geometry at short source-detector separations. In addition, the probing depth of the MTL geometry is smaller than that of the semi-infinite geometry at a same source-detector separation.

We then demonstrated the relationship between the interrogation depth and several parameters of the superficial diffusing probe in MTL geometry, including sample optical properties, source-detector separations, and the properties of the diffusing slab. The results from Monte Carlo simulations illustrate that the optical properties of the samples play a significant role in modulating the interrogation depth of the diffusing probe.

The two dominant probe parameters that influence the interrogation depth of a diffusing probe are the source-detector separation and the thickness of the scattering layer. The average interrogation depth of the diffusing probe varies linearly with the source-detector separation in the range from 1 to 5 mm. The diffusing probe generally has shallower interrogation depth than a conventional DOS probe at a same source-detector separation. In addition, as shown in Figs. 10 and 11, the dependence of the interrogation depths on the source-detector separation of the diffusing probe is weaker than that of a semi-infinite geometry probe. Although the thickness of the scattering layer has an effect on the interrogation depth, we illustrated that the magnitude of this effect depends on the source-detector separation. To choose a proper scattering layer thickness for a diffusing probe, both the validity of the diffusion approximation and the probe reliability should be taken into consideration.

On the other hand, the dependence of the interrogation depths on the NA of detection fiber is much weaker than that of a semi-infinite geometry probe. Thus, the NA of the detection fiber is not an efficient parameter that can be used to
control the interrogation depth. While the optical properties, including absorption coefficient, reduced scattering coefficient, and asymmetry factor, of the diffusing slab have a negligible influence on the interrogation depth, they can greatly affect the photon detection efficiency. Our simulation results provide guidelines for designing a diffusing probe with a specific average interrogation depth for various clinical applications, including skin hydration measurements, monitoring of specific average interrogation depth for various clinical applications.

Acknowledgments

Dr. Tseng would like to acknowledge the support provided by the National Science Council of Taiwan under Grant No. NSC-98-2218-E-006-013. Dr. Durkin is supported by the National Science Council of Taiwan under Grant No. 98-2218-E-006-013. Dr. Tseng would like to acknowledge the support provided by the National Science Council of Taiwan under Grant No. 98-2218-E-006-013. Dr. Tseng would like to acknowledge the support provided by the National Science Council of Taiwan under Grant No. 98-2218-E-006-013.

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